

FOURIER ANALYSIS AN INTRODUCTION

FOURIER ANALYSIS AN INTRODUCTION PRESENTS A FOUNDATIONAL OVERVIEW OF ONE OF THE MOST POWERFUL MATHEMATICAL TOOLS USED IN SIGNAL PROCESSING, PHYSICS, AND ENGINEERING. THIS ARTICLE EXPLORES THE CORE CONCEPTS BEHIND FOURIER ANALYSIS, EXPLAINING HOW COMPLEX SIGNALS CAN BE DECOMPOSED INTO SIMPLER SINUSOIDAL COMPONENTS. THE DISCUSSION COVERS THE MATHEMATICAL BASIS OF THE FOURIER TRANSFORM, ITS VARIANTS, AND PRACTICAL APPLICATIONS ACROSS VARIOUS SCIENTIFIC FIELDS. EMPHASIS IS PLACED ON UNDERSTANDING THE SIGNIFICANCE OF FREQUENCY DOMAIN REPRESENTATION AND THE ADVANTAGES IT OFFERS OVER TIME-DOMAIN ANALYSIS. THIS INTRODUCTION ALSO ADDRESSES THE COMPUTATIONAL METHODS EMPLOYED IN FOURIER ANALYSIS, INCLUDING THE FAST FOURIER TRANSFORM (FFT) ALGORITHM. READERS WILL GAIN A CLEAR UNDERSTANDING OF THE THEORETICAL FRAMEWORK AND PRACTICAL UTILITY OF FOURIER ANALYSIS, PREPARING THEM FOR MORE ADVANCED STUDIES OR APPLICATIONS. BELOW IS A DETAILED TABLE OF CONTENTS OUTLINING THE TOPICS COVERED.

- FUNDAMENTALS OF FOURIER ANALYSIS
- MATHEMATICAL FOUNDATIONS
- TYPES OF FOURIER TRANSFORMS
- APPLICATIONS OF FOURIER ANALYSIS
- COMPUTATIONAL TECHNIQUES

FUNDAMENTALS OF FOURIER ANALYSIS

FOURIER ANALYSIS IS CENTERED ON THE IDEA THAT ANY COMPLEX WAVEFORM CAN BE REPRESENTED AS A SUM OF SIMPLER SINE AND COSINE WAVES. THIS PRINCIPLE IS CRUCIAL FOR UNDERSTANDING SIGNALS IN TERMS OF THEIR FREQUENCY COMPONENTS RATHER THAN JUST THEIR TIME-DOMAIN BEHAVIOR. THE PROCESS INVOLVES DECOMPOSING A SIGNAL INTO ITS CONSTITUENT FREQUENCIES, WHICH PROVIDES INSIGHT INTO THE SIGNAL'S STRUCTURE AND PROPERTIES. FOURIER ANALYSIS SERVES AS A BRIDGE BETWEEN TIME AND FREQUENCY DOMAINS, ENABLING EASIER MANIPULATION AND INTERPRETATION OF DATA.

HISTORICAL BACKGROUND

THE CONCEPT OF FOURIER ANALYSIS ORIGINATED FROM THE WORK OF JEAN-BAPTISTE JOSEPH FOURIER IN THE EARLY 19TH CENTURY. FOURIER INTRODUCED THE IDEA THAT HEAT TRANSFER AND OTHER PHYSICAL PHENOMENA COULD BE DESCRIBED BY SUMS OF TRIGONOMETRIC FUNCTIONS. HIS GROUNDBREAKING WORK LED TO THE FORMAL DEVELOPMENT OF FOURIER SERIES AND TRANSFORMS, WHICH HAVE SINCE BECOME INDISPENSABLE TOOLS IN MATHEMATICS AND ENGINEERING.

BASIC PRINCIPLE

AT ITS CORE, FOURIER ANALYSIS RELIES ON THE ORTHOGONALITY OF SINE AND COSINE FUNCTIONS. ANY PERIODIC SIGNAL CAN BE EXPRESSED AS AN INFINITE SUM OF SINE AND COSINE TERMS WITH DIFFERENT FREQUENCIES, AMPLITUDES, AND PHASES. THIS DECOMPOSITION ALLOWS THE SIGNAL TO BE ANALYZED IN TERMS OF ITS FREQUENCY SPECTRUM, REVEALING HIDDEN PERIODICITIES AND CHARACTERISTICS NOT EASILY OBSERVED IN THE TIME DOMAIN.

MATHEMATICAL FOUNDATIONS

THE MATHEMATICAL FRAMEWORK OF FOURIER ANALYSIS INVOLVES SEVERAL KEY CONCEPTS AND FORMULAS THAT DEFINE HOW SIGNALS ARE TRANSFORMED AND RECONSTRUCTED. UNDERSTANDING THESE FOUNDATIONS IS ESSENTIAL FOR APPLYING FOURIER TECHNIQUES EFFECTIVELY.

FOURIER SERIES

THE FOURIER SERIES EXPRESSES A PERIODIC FUNCTION AS A SUM OF SINE AND COSINE TERMS. FOR A FUNCTION $f(t)$ WITH PERIOD T , THE FOURIER SERIES IS GIVEN BY:

- CONSTANT TERM REPRESENTING THE AVERAGE VALUE
- SINE AND COSINE TERMS WITH FREQUENCIES THAT ARE INTEGER MULTIPLES OF THE FUNDAMENTAL FREQUENCY ($1/T$)

THIS SERIES CONVERGES TO THE ORIGINAL FUNCTION UNDER CERTAIN CONDITIONS AND PROVIDES A FREQUENCY DOMAIN REPRESENTATION OF PERIODIC SIGNALS.

FOURIER TRANSFORM

THE FOURIER TRANSFORM GENERALIZES THE FOURIER SERIES FOR NON-PERIODIC FUNCTIONS. IT CONVERTS A TIME-DOMAIN SIGNAL INTO A CONTINUOUS FREQUENCY SPECTRUM, ALLOWING ANALYSIS OF SIGNALS THAT ARE NOT NECESSARILY PERIODIC. THE TRANSFORM IS DEFINED AS AN INTEGRAL THAT MAPS A FUNCTION FROM THE TIME DOMAIN TO THE FREQUENCY DOMAIN, REVEALING THE AMPLITUDE AND PHASE OF EACH FREQUENCY COMPONENT.

INVERSE FOURIER TRANSFORM

THE INVERSE FOURIER TRANSFORM RECONSTRUCTS THE ORIGINAL TIME-DOMAIN SIGNAL FROM ITS FREQUENCY REPRESENTATION. THIS REVERSIBILITY IS FUNDAMENTAL TO THE PRACTICAL USE OF FOURIER ANALYSIS, ENSURING THAT NO INFORMATION IS LOST DURING TRANSFORMATION.

TYPES OF FOURIER TRANSFORMS

SEVERAL VARIATIONS OF THE FOURIER TRANSFORM EXIST, EACH SUITED TO DIFFERENT TYPES OF DATA AND APPLICATIONS. UNDERSTANDING THESE VARIANTS HELPS IN SELECTING THE APPROPRIATE TRANSFORM FOR SPECIFIC ANALYTICAL NEEDS.

CONTINUOUS FOURIER TRANSFORM (CFT)

THE CONTINUOUS FOURIER TRANSFORM IS USED FOR CONTINUOUS-TIME SIGNALS AND PROVIDES A CONTINUOUS SPECTRUM OF FREQUENCIES. IT IS WIDELY APPLIED IN THEORETICAL PHYSICS AND ENGINEERING PROBLEMS INVOLVING CONTINUOUS SIGNALS.

DISCRETE FOURIER TRANSFORM (DFT)

THE DISCRETE FOURIER TRANSFORM APPLIES TO DISCRETE-TIME SIGNALS, SUCH AS DIGITAL DATA SAMPLES. IT CONVERTS A FINITE SEQUENCE OF EQUALLY SPACED SAMPLES INTO A DISCRETE FREQUENCY SPECTRUM. THE DFT IS PARTICULARLY IMPORTANT IN DIGITAL SIGNAL PROCESSING.

FAST FOURIER TRANSFORM (FFT)

THE FAST FOURIER TRANSFORM IS AN EFFICIENT ALGORITHM FOR COMPUTING THE DFT. BY REDUCING COMPUTATIONAL COMPLEXITY FROM $O(N^2)$ TO $O(N \log N)$, THE FFT ENABLES RAPID PROCESSING OF LARGE DATASETS AND REAL-TIME SIGNAL ANALYSIS. IT IS A FUNDAMENTAL TOOL IN MODERN DIGITAL COMMUNICATIONS AND IMAGE PROCESSING.

APPLICATIONS OF FOURIER ANALYSIS

FOURIER ANALYSIS FINDS EXTENSIVE USE ACROSS VARIOUS DISCIPLINES DUE TO ITS ABILITY TO SIMPLIFY COMPLEX SIGNALS AND REVEAL FREQUENCY CONTENT. ITS VERSATILITY MAKES IT A CORNERSTONE TECHNIQUE IN BOTH THEORETICAL AND APPLIED SCIENCES.

SIGNAL PROCESSING

IN SIGNAL PROCESSING, FOURIER ANALYSIS IS USED TO FILTER NOISE, COMPRESS DATA, AND ANALYZE FREQUENCY COMPONENTS OF AUDIO, RADAR, AND COMMUNICATION SIGNALS. IT HELPS IN DESIGNING FILTERS AND SYSTEMS THAT OPERATE EFFICIENTLY IN THE FREQUENCY DOMAIN.

IMAGE PROCESSING

FOURIER TRANSFORMS ARE EMPLOYED TO ENHANCE IMAGES, DETECT EDGES, AND REMOVE NOISE. FREQUENCY DOMAIN PROCESSING ALLOWS FOR MANIPULATION OF IMAGE CHARACTERISTICS THAT ARE DIFFICULT TO ADDRESS IN THE SPATIAL DOMAIN.

ELECTRICAL ENGINEERING

FOURIER ANALYSIS ASSISTS IN ANALYZING ELECTRICAL CIRCUITS AND SYSTEMS BY STUDYING THEIR FREQUENCY RESPONSE. IT IS CRITICAL FOR THE DESIGN OF AMPLIFIERS, OSCILLATORS, AND SIGNAL MODULATORS.

PHYSICS AND ASTRONOMY

THE TECHNIQUE IS USED TO ANALYZE WAVEFORMS IN QUANTUM MECHANICS, OPTICS, AND ASTROPHYSICS. FOURIER METHODS HELP INTERPRET SIGNALS FROM TELESCOPES AND OTHER SENSING EQUIPMENT, PROVIDING INSIGHTS INTO THE PROPERTIES OF DISTANT OBJECTS.

COMPUTATIONAL TECHNIQUES

EFFECTIVE COMPUTATION OF FOURIER TRANSFORMS IS ESSENTIAL FOR PRACTICAL APPLICATIONS. ADVANCES IN ALGORITHMS AND SOFTWARE HAVE MADE FOURIER ANALYSIS ACCESSIBLE AND EFFICIENT FOR LARGE-SCALE DATA.

ALGORITHMIC EFFICIENCY

THE FAST FOURIER TRANSFORM ALGORITHM REVOLUTIONIZED COMPUTATIONAL FOURIER ANALYSIS BY DRASTICALLY REDUCING THE NUMBER OF CALCULATIONS REQUIRED. THIS EFFICIENCY ALLOWS REAL-TIME PROCESSING IN APPLICATIONS LIKE AUDIO SIGNAL FILTERING AND TELECOMMUNICATIONS.

SOFTWARE IMPLEMENTATIONS

NUMEROUS SOFTWARE LIBRARIES AND TOOLS IMPLEMENT FOURIER TRANSFORMS, PROVIDING RELIABLE AND OPTIMIZED FUNCTIONS FOR ENGINEERS AND SCIENTISTS. THESE IMPLEMENTATIONS SUPPORT VARIOUS DATA TYPES AND OFFER FLEXIBILITY FOR CUSTOMIZED ANALYSIS.

CHALLENGES AND CONSIDERATIONS

PRACTICAL COMPUTATION OF FOURIER TRANSFORMS MUST ADDRESS ISSUES SUCH AS SPECTRAL LEAKAGE, WINDOWING EFFECTS, AND NUMERICAL PRECISION. PROPER HANDLING OF THESE CHALLENGES ENSURES ACCURATE FREQUENCY DOMAIN REPRESENTATIONS.

1. UNDERSTANDING SIGNAL PROPERTIES TO CHOOSE APPROPRIATE WINDOW FUNCTIONS
2. SAMPLING AT ADEQUATE RATES TO AVOID ALIASING
3. APPLYING ZERO-PADDING TO IMPROVE FREQUENCY RESOLUTION

FREQUENTLY ASKED QUESTIONS

WHAT IS FOURIER ANALYSIS AND WHY IS IT IMPORTANT?

FOURIER ANALYSIS IS A MATHEMATICAL METHOD THAT DECOMPOSES FUNCTIONS OR SIGNALS INTO FREQUENCIES OR SINE AND COSINE COMPONENTS. IT IS IMPORTANT BECAUSE IT ALLOWS FOR THE ANALYSIS AND PROCESSING OF SIGNALS IN VARIOUS FIELDS SUCH AS ENGINEERING, PHYSICS, AND APPLIED MATHEMATICS.

WHAT ARE THE BASIC CONCEPTS INTRODUCED IN 'FOURIER ANALYSIS: AN INTRODUCTION'?

THE BOOK COVERS FOUNDATIONAL CONCEPTS INCLUDING FOURIER SERIES, FOURIER TRANSFORMS, CONVERGENCE THEOREMS, AND APPLICATIONS OF FOURIER METHODS TO DIFFERENTIAL EQUATIONS AND SIGNAL PROCESSING.

How does Fourier series differ from Fourier transform in Fourier analysis?

Fourier series represents periodic functions as sums of sine and cosine functions with discrete frequencies, while Fourier transform generalizes this to non-periodic functions by representing them as continuous integrals over frequencies.

What prerequisites are recommended before studying 'Fourier Analysis: An Introduction'?

A solid understanding of calculus, including integration and differentiation, as well as basic knowledge of linear algebra and complex numbers, is recommended before studying Fourier analysis.

How is Fourier analysis applied in real-world scenarios?

Fourier analysis is used in signal processing, image compression, audio analysis, solving partial differential equations, and even in quantum physics to analyze wave functions and frequency components.

Additional Resources

1. *Fourier Analysis: An Introduction* by Elias M. Stein and Rami Shakarchi

This book offers a clear and comprehensive introduction to Fourier analysis, suitable for advanced undergraduates and beginning graduate students. It covers the basics of Fourier series, Fourier transforms, and their applications in various fields. The text balances theory and practical applications, providing numerous examples and exercises to solidify understanding.

2. *Fourier Series and Integrals* by H. Dym and H.P. McKean

A classic text that explores the theory of Fourier series and integrals with rigor and clarity. The book emphasizes the connection between Fourier analysis and differential equations, making it valuable for students in mathematics and engineering. It includes detailed proofs and a variety of problems to enhance problem-solving skills.

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This book introduces fundamental concepts in Fourier analysis alongside wavelet theory, providing a broader perspective on signal processing techniques. It is well-suited for students with a background in calculus and linear algebra. The author uses intuitive explanations and visual illustrations to make complex ideas more accessible.

4. *Fourier Analysis* by T.W. Körner

Körner's text is known for its engaging style and thorough treatment of classical Fourier analysis topics. It covers Fourier series, transforms, and applications, with an emphasis on problem-solving and real-world examples. The book is designed to be accessible to readers new to the subject while still offering depth for more advanced learners.

5. *A First Course in Fourier Analysis* by David W. Kammler

This introductory book provides a balanced approach between theory and applications of Fourier analysis. It includes topics such as Fourier series, transforms, and discrete Fourier analysis, with numerous examples drawn from engineering and physics. The clear explanations make it suitable for students in a variety of scientific disciplines.

6. *Fourier Analysis: Theory and Applications* by Anders Vretblad

Vretblad's work offers a concise yet thorough introduction to both the theoretical and practical aspects of Fourier analysis. The book covers classical Fourier series and transforms, as well as applications to differential equations and signal processing. Exercises and examples help reinforce the concepts presented.

7. *Applied Fourier Analysis* by Tim Olson

Focusing on applications, this book introduces Fourier analysis concepts with an emphasis on their use in

ENGINEERING AND THE PHYSICAL SCIENCES. THE TEXT INCLUDES DISCUSSIONS ON FOURIER SERIES, TRANSFORMS, AND NUMERICAL METHODS IN FOURIER ANALYSIS. IT IS IDEAL FOR STUDENTS LOOKING TO APPLY FOURIER TECHNIQUES TO REAL-WORLD PROBLEMS.

8. *FOURIER ANALYSIS AND ITS APPLICATIONS* BY GERALD B. FOLLAND

FOLLAND'S BOOK IS A WELL-REGARDED INTRODUCTION THAT COMBINES RIGOROUS MATHEMATICAL TREATMENT WITH PRACTICAL APPLICATIONS. IT COVERS CLASSICAL FOURIER ANALYSIS, DISTRIBUTION THEORY, AND MODERN EXTENSIONS, MAKING IT SUITABLE FOR ADVANCED UNDERGRADUATES AND GRADUATE STUDENTS. THE TEXT INCLUDES A WEALTH OF EXERCISES TO DEVELOP A DEEP UNDERSTANDING OF THE MATERIAL.

9. *FOURIER SERIES* BY GEORGI P. TOLSTOV

THIS CLASSIC TEXT PROVIDES A THOROUGH INTRODUCTION TO FOURIER SERIES WITH A FOCUS ON FOUNDATIONAL THEORY AND DETAILED PROOFS. IT IS KNOWN FOR ITS CLARITY AND SYSTEMATIC APPROACH, MAKING IT A VALUABLE RESOURCE FOR STUDENTS BEGINNING THEIR STUDY OF FOURIER ANALYSIS. THE BOOK ALSO INCLUDES HISTORICAL CONTEXT AND APPLICATIONS TO VARIOUS MATHEMATICAL PROBLEMS.

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century when studying problems in the physical sciences--that an arbitrary function can be written as an infinite sum of the most basic trigonometric functions. The first part implements this idea in terms of notions of convergence and summability of Fourier series, while highlighting applications such as the isoperimetric inequality and equidistribution. The second part deals with the Fourier transform and its applications to classical partial differential equations and the Radon transform; a clear introduction to the subject serves to avoid technical difficulties. The book closes with Fourier theory for finite abelian groups, which is applied to prime numbers in arithmetic progression. In organizing their exposition, the authors have carefully balanced an emphasis on key conceptual insights against the need to provide the technical underpinnings of rigorous analysis. Students of mathematics, physics, engineering and other sciences will find the theory and applications covered in this volume to be of real interest. The Princeton Lectures in Analysis represents a sustained effort to introduce the core areas of mathematical analysis while also illustrating the organic unity between them. Numerous examples and applications throughout its four planned volumes, of which Fourier Analysis is the first, highlight the far-reaching consequences of certain ideas in analysis to other fields of mathematics and a variety of sciences. Stein and Shakarchi move from an introduction addressing Fourier series and integrals to in-depth considerations of complex analysis; measure and integration theory, and Hilbert spaces; and, finally, further topics such as functional analysis, distributions and elements of probability theory.

fourier analysis an introduction: Fourier Analysis : an Introduction , 2003

fourier analysis an introduction: Introduction to Fourier Analysis and Wavelets Mark A.

Pinsky, 2023-12-21 This book provides a concrete introduction to a number of topics in harmonic analysis, accessible at the early graduate level or, in some cases, at an upper undergraduate level. Necessary prerequisites to using the text are rudiments of the Lebesgue measure and integration on the real line. It begins with a thorough treatment of Fourier series on the circle and their applications to approximation theory, probability, and plane geometry (the isoperimetric theorem). Frequently, more than one proof is offered for a given theorem to illustrate the multiplicity of approaches. The second chapter treats the Fourier transform on Euclidean spaces, especially the author's results in the three-dimensional piecewise smooth case, which is distinct from the classical Gibbs-Wilbraham phenomenon of one-dimensional Fourier analysis. The Poisson summation formula treated in Chapter 3 provides an elegant connection between Fourier series on the circle and Fourier transforms on the real line, culminating in Landau's asymptotic formulas for lattice points on a large sphere. Much of modern harmonic analysis is concerned with the behavior of various linear operators on the Lebesgue spaces $L^p(\mathbb{R}^n)$. Chapter 4 gives a gentle introduction to these results, using the Riesz-Thorin theorem and the Marcinkiewicz interpolation formula. One of the long-time users of Fourier analysis is probability theory. In Chapter 5 the central limit theorem, iterated log theorem, and Berry-Esseen theorems are developed using the suitable Fourier-analytic tools. The final chapter furnishes a gentle introduction to wavelet theory, depending only on the L_2 theory of the Fourier transform (the Plancherel theorem). The basic notions of scale and location parameters demonstrate the flexibility of the wavelet approach to harmonic analysis. The text contains numerous examples and more than 200 exercises, each located in close proximity to the related theoretical material.

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M. Stein, Guido Weiss, 2016-06-02 The authors present a unified treatment of basic topics that arise in Fourier analysis. Their intention is to illustrate the role played by the structure of Euclidean spaces, particularly the action of translations, dilatations, and rotations, and to motivate the study of harmonic analysis on more general spaces having an analogous structure, e.g., symmetric spaces.

fourier analysis an introduction: An Introduction to Fourier Analysis Russell L. Herman,

2016-09-19 This book helps students explore Fourier analysis and its related topics, helping them appreciate why it pervades many fields of mathematics, science, and engineering. This introductory textbook was written with mathematics, science, and engineering students with a background in

calculus and basic linear algebra in mind. It can be used as a textbook for undergraduate courses in Fourier analysis or applied mathematics, which cover Fourier series, orthogonal functions, Fourier and Laplace transforms, and an introduction to complex variables. These topics are tied together by the application of the spectral analysis of analog and discrete signals, and provide an introduction to the discrete Fourier transform. A number of examples and exercises are provided including implementations of Maple, MATLAB, and Python for computing series expansions and transforms. After reading this book, students will be familiar with: • Convergence and summation of infinite series • Representation of functions by infinite series • Trigonometric and Generalized Fourier series • Legendre, Bessel, gamma, and delta functions • Complex numbers and functions • Analytic functions and integration in the complex plane • Fourier and Laplace transforms. • The relationship between analog and digital signals Dr. Russell L. Herman is a professor of Mathematics and Professor of Physics at the University of North Carolina Wilmington. A recipient of several teaching awards, he has taught introductory through graduate courses in several areas including applied mathematics, partial differential equations, mathematical physics, quantum theory, optics, cosmology, and general relativity. His research interests include topics in nonlinear wave equations, soliton perturbation theory, fluid dynamics, relativity, chaos and dynamical systems.

fourier analysis an introduction: Introduction to Fourier Analysis Norman Morrison, 1994-12-13 Contains 36 lectures solely on Fourier analysis and the FFT. Time and frequency domains, representation of waveforms in terms of complex exponentials and sinusoids, convolution, impulse response and the frequency transfer function, modulation and demodulation are among the topics covered. The text is linked to a complete FFT system on the accompanying disk where almost all of the exercises can be either carried out or verified. End-of-chapter exercises have been carefully constructed to serve as a development and consolidation of concepts discussed in the text.

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fourier analysis an introduction: An Introduction to Fourier Analysis and Generalised Functions Sir M. J. Lighthill, 1958 Clearly and attractively written, but without any deviation from rigorous standards of mathematical proof.... Science Progress

fourier analysis an introduction: An Introduction to Basic Fourier Series Sergei Suslov, 2013-03-09 It was with the publication of Norbert Wiener's book "The Fourier Integral and Certain of Its Applications [165] in 1933 by Cambridge University Press that the mathematical community came to realize that there is an alternative approach to the study of classical Fourier Analysis, namely, through the theory of classical orthogonal polynomials. Little would he know at that time that this little idea of his would help usher in a new and exiting branch of classical analysis called q-Fourier Analysis. Attempts at finding q-analogs of Fourier and other related transforms were made

by other authors, but it took the mathematical insight and instincts of none other than Richard Askey, the grand master of Special Functions and Orthogonal Polynomials, to see the natural connection between orthogonal polynomials and a systematic theory of q -Fourier Analysis. The paper that he wrote in 1993 with N. M. Atakishiyev and S. K. Suslov, entitled An Analog of the Fourier Transform for a q -Harmonic Oscillator [13], was probably the first significant publication in this area. The Poisson kernel for the continuous q -Hermite polynomials plays a role of the q -exponential function for the analog of the Fourier integral under consideration; see also [14] for an extension of the q -Fourier transform to the general case of Askey-Wilson polynomials. (Another important ingredient of the q -Fourier Analysis, that deserves thorough investigation, is the theory of q -Fourier series.

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